Appropriate Volume Functions for Leguminosae Family in Two Tropical Rainforests in Cross River State, Nigeria

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Abstract

Volume equations were developed for tree species of leguminosae family in two tropical rainforest, Nigeria. The data used consist of merchantable volume, stump diameter, diameter at breast height and merchantable height for 22 tree species. The number of observations per species ranged from 1 to 30 while the diameter at breast height ranged from 10.00 cm to 132.20 cm. The result in this study shows that generalised logarithmic volume function (also termed Schumacher’s volume function) performed better than other forms of volume functions. For example, the best adjudged volume for all species combined were $lnV = -0.48205 + 0.9939\ln(Dbh^2H)$ and $lnV = -0.78963 + 1.0391Dst^2H$. The merchantable volume developed from double-variable function indicates negative intercept while the single-variable volume function represents the logarithmic nonlinear function and performed best within the limit of data used for each species group. The method of species grouping in this study was morphological and was based on sub-families of tree species.
results indicate that $D^2H$ as weighting factor was found to be appropriate in reducing heteroscedasticity. The model being significant indicates a good fits and confirmed the effectiveness of weighted predictor in stabilising error variance. The resulting volume functions possessed desirable statistical properties and model behaviours, and can be used to estimate timber volume in the tropical rain forest areas of Nigeria. The volume equations based on stump diameter alone are adequate to provide estimates of tree volume illegally removed.

**Keywords:** Volume equation, Species grouping, Modelling, Mixed tropical forest
1. Introduction

The heterogeneity and high species diversity makes it difficult to understand and predict complex nature of mixed tropical forest. According to Gourlet-Fleury et al., (2005), this difficulty hinders the development of predictive dynamic models, essential for forest managers to simulate logging scenarios for sustainable exploitation. Modeling methodology not only has moved from an empirical approach to a more ecological process-based mechanistic approach, but also has incorporated a variety of techniques due to the dynamic biological systems of mixed tropical forest that are continuously changing (Peng, 1999).

There is always a setback in developing separate set of equations for each species due to the existing conditions in the tropical forests and the nature of their dataset. In particular, many species lack sufficient data for reliable estimation of model parameters. On the other hand, pooling together the entire data set of all species for the purpose of fitting volume functions will result in a very large error variance (Akindele and LeMay, 2006). Consequently, the common approach used for modeling forest data is to aggregate species into several groups, and develop separate equations for each group. According to Akindele, (2005), this approach has been used by several authors including Swaine and Whitmore (1988), Vanclay (1991), Chai and LeMay (1993), Atta-Boateng and Moser (1998), Favrichon (1998), Finegan et al. (1999), Gourlet-Fleury and Houllier (2000), Huth and Ditzer (2001) Phillips et al. (2002), Picard and Franc (2003), and Zhao et al. (2004). Grouping the species helps to avoid the need for specific equations for species with few data, and also facilitates a reduction in the number of functions to a more manageable number (Vanclay, 1991).

Various techniques have been proposed for grouping trees in mixed-species stands. According to Gitay and Noble (1997), there is no universally applicable concept for aggregating species into groups. The type of classification depends on the context of the performed aggregation (Kohler, et al., 2000) and the type of data available (Akindele, 2005). For example, Porte and Bartelink (2002) analysed various criteria that have been used to classify the models. Gourlet-Fleury et al., (2005) suggested three strategies for grouping species for the purpose of modelling in tropical rainforest, they are:

1) Ecological subjective groups;
2) Ecological data-driven groups and
3) Dynamic process groups (corresponding to the components of forest dynamics: recruitment, growth, mortality).

Due to complexity of tropical rainforest, hence there is a need to examine other methods of grouping species. In this study, classification will be based on characteristics community dynamics in terms of sub-families. That means, modelling the tree volume will be based on some properties of the tree characters used for grouping species and this is due to lack of dynamic data to correctly assign each species to a group. The driven force for grouping species in this study is closeness in intra-specific variability of the characters of the tree species. In this case, similarity in physiological and morphological characteristic will be taken into cognisance in grouping the species. This method of species grouping ensures that
species are classified according to ecomorphological attributes of the sub-family.

The objectives of this study were to aggregate leguminosae species in two tropical rainforests into sub-family groups and develop appropriate tree volume equations for each group of species. It is hoped that the equations will serve as efficient tools for obtaining reliable estimates of growing stock in the tropical rain forest ecosystem.

2. Methodology

2.1 Study Area

This study was conducted in the Afi River and Oban Forest Reserves which are located in Cross River State (Fig. 1). The forests are considered as biodiversity hotspot of global significance (Myers et al. 2000, Oates et al. 2004).

2.1.1 Afi River Forest Reserve

Afi River Forest Reserve lies approximately between latitudes 6° 08’ and 6° 26’N and longitudes 8° 50’ and 9° 05’E and covers a total land area of 383.32 km² including the area known as Afi Mountain. The topography is extremely complex with many connected ridge systems, isolated peaks and outcrops, and ranging between 200m - 1200m above sea level.
The reserve is characterized by large tracts of rock outcrops especially on the North-East axis. The hills of the reserve are extension of the Cameroon Mountains geological formation. The fast moving and high gradient streams drain the Afi River Forest Reserve, constituting an important watershed. The geological and soil components can be described as crustaceous sedimentary sandstone occupying a significant area of the study site. In a few places, there are volcanic eruptions through the sedimentary surface and this sometimes comprises columnar basalt (Nsor, 2004).

The Information on the soils of the area is not well documented. Old sedimentary soils tend to be sandy with structure less profiles and incipient laterite. Generally the soils vary from clayey-loam to loamy-clay and normally red with high content of iron oxide. The soils are generally acidic and of low nutrient status, thus not suitable for arable crop production (Agbor, 2003). The entire area falls within a broad annual rain fall zone of 3,000 mm - 3,800 mm but, with a variation increasing from lowland to uphill (Agbor, 2003). The mean temperatures on Afi Mountain was 22.2°C, and in the lowland 27.4°C. Daily minimum temperatures on Afi Mountain averaged 18.7°C and in the lowland 22.1°C while an average of 25.8°C and 32.8°C were recorded as daily maximum temperatures for Afi Mountain and its lowland respectively. Though data on relative humidity, evapo-transpiration and water budgets were never recorded in and around the reserve, but the work of Balogun, (2003) indicate that the mean annual relative humidity is 78% at 7.00 Hr.

The vegetation of Afi River Forest Reserve generally falls within the tropical high forest vegetation zone. The rainforest occupies the foot of the mountain and at about 700m part of the forest structure changes gradually into sub-montane vegetation, while above 500m, parts of the vegetation have been changed into grassland as a result of annual bush fire (Agbor, 2003).

2.1.2 Oban Forest Reserve

Oban group forest reserve also known as Oban block forest reserve lies within longitude 8°20′ E and 8°55′ E and latitudes 5°00′ N and 6°00′ N. Presently, it cover an area of 742.55km². Topographically, the terrain is rugged and its elevation rises from the river valleys to over 1,000 m in mountainous areas (Jimoh et al., 2012). Most of the area is characterized by hilly terrain ranging from 100 to over 1,000m. Greater elevation is accompanied by increased dissection and structural control of drainage. Within the more mountainous areas a rectangular drainage pattern is always noticed. Oban Forest Reserve consists of dominant rock types that are ancient metamorphic rocks of the Basement Complex which cover 50% of Nigeria. Derived from sedimentary rocks and Precambrian in age these rocks are interspersed with smaller areas of intrusive igneous rocks. The metamorphic rocks are mainly gneisses (biotite-hornblende, granite and migmatitic gneiss and to a lesser extent amphibolite (schist). (Holland et al, 1989; Schmitt, 1996).

Less sandy soils are found in areas with igneous rocks and deeper soils prevail in the plains of the southern part of the park whilst on steeper slopes they are increasingly stony, shallow and erodible (Holland et al, 1989). The annual rainfall is generally, between 2,500mm-3,000mm. At times, it can be up to 4,000mm. Temperatures are generally high (average...
around 27º C) and vary little throughout the year with the annual range of the monthly average temperature varying only between 3º and 3.5º C. Mean monthly relative humidity varies between 78% and 91% with an average of 85%. (Holland et al, 1989; Schmitt, 1996).

2.2 Data Collection

Multistage sampling method was adopted in this study. This sampling procedure was made up of primary, secondary and tertiary sampling units. 1000m by 1000m, were randomly chosen, which constitute the primary units. The primary units were divided into secondary 20 units of rectangular plots (otherwise known as strip plot) of 50 m by 1000 m (5 ha in size), out of which about 4 plots were randomly chosen. The strip plot is a form of rectangular plot often used in tropical rainforest inventory (Colwell, 2009). Each selected secondary units (strip plot) were then divided into 25 equal tertiary plots of 40 m by 50 m (0.2ha) in size, out of which 4 plots were randomly selected. Consequently, the total numbers of sampling plots (tertiary units) for this study were 24 sampling plots. Tree identification and detailed growing stock assessment were undertaken within the tertiary sampling units. The following measurements were made on sampled trees within each of the selected temporary sample plot (i.e. tertiary unit):

i. Outside bark stump diameter (Dst)(cm) at 15 cm above ground (since a survey of past exploitation showed that no tree is cut below this point) (Akindele, 2003),

ii. Merchantable height (MHT)/m (which is the point between ground level and point of the first surviving whorl of branch),

iii. Outside bark diameter measurements, at base, middle and top positions (taken at a point close to the first surviving whorl of branch).

iv. Outside bark diameter at breast height (Dbh) (taken at 1.3m from ground) of trees whose diameter is greater than or equal to 10 cm.

2.3 Data Analysis

2.3.1 Preliminary Data Analysis

The initial analysis of the data involves the computation of individual tree basal area and volume from the raw data as well as their extrapolation to per-hectare estimates. The individual tree volumes were estimated for the merchantable portion and total stem; the procedures include the following steps.

(1) Computation of basal area of all individual trees using equation 1:

\[ BA = \frac{\pi D^2}{4} \]  

Where \( BA \) = basal area (m\(^2\))

\( \pi \) = 3.142 (a constant)

\( D \) = Dbh (m)
Basal area per plot was obtained by adding the basal area of all individual trees within the plot. Mean plot basal area were computed by summing the total plot basal areas of the sample plots selected from the primary unit and dividing by the number of sample plots selected from that primary unit. Basal area per hectare was then obtained by multiplying the mean plot basal area by the number of sample plots per hectare.

(2) The volume of individual trees in each plot were computed using Newton’s formula (Husch et al., 2003)

\[ V = \frac{h}{6}(A_b + 4A_m + A_t) \]  

Where:

- \( V \) = tree volume (\( m^3 \))
- \( h \) = tree height (m)
- \( A_b \) = Cross-sectional area at the base (\( m^2 \))
- \( A_t \) = Cross-sectional area at the top (\( m^2 \))
- \( A_m \) = Cross-sectional area at the middle (\( m^2 \))

Volume per plot was obtained by adding the volume of all individual trees within the plot. Mean plot volume were then computed by summing the total volumes of the sample plots selected from the primary unit and dividing by the number of sample plots selected from that primary unit. Volume per hectare was obtained by multiplying the mean plot volume by the number of sample plots per hectare. Following the computation of tree volume and other related variable, the data were summarized by computing simple statistics for each species. The statistics included number of observations per hectare, range, mean and standard error of the mean. Graphs for the species grouped data were also plotted to examine the relationship between the variables.

2.3.2 Volume Equations for All Species Combined

In order to have a benchmark with which to compare equations in other categories, several equations were fitted to the combined data set after aggregating all the species into one group. The best equation was chosen to developed volume equation for all species combined.

2.3.3 Volume Equations for Groups of Species

All species within same sub-family formed the basis for species grouping. In overall, all the species were grouped into 3 groups based on the number of leguminosae sub-families identified in the two forest reserve. Tree species within each sub-family group were pooled together and tree volume functions were then fitted for each group of species. Series of volume functions were fitted and compared. The equation that produced unbiased estimates as well as residual plots that shows conformity with the assumption of independence of errors...
was considered. Volume equations were developed separately from diameter at breast height (dbh) and stump diameter multivariable for each group. These were considered important from practical point of view.

The volume equation based on stump diameter alone is particularly useful in instances where there is the problem of illegal logging activities, leaving only the stump (Akindele, 1987, 2003). This equation will make it possible to obtain estimates of merchantable volume lost to such illegal activities.

After several trials and comparison of different model forms, the models fitted were weighted quadratic models. They performed best in terms of the fit statistics and randomness of the residuals over the entire range of volume prediction. Some of the several model tried were:

\[
V = \beta_1 D^2 H + \varepsilon_i \quad \text{----------------------------- (3)}
\]

\[
V = \alpha_0 + \beta_1 D^2 H + \varepsilon_i \quad \text{----------------------------- (4)}
\]

\[
\ln V = \alpha_0 + \beta_1 \ln D \ln H + \varepsilon_i \quad \text{----------------------------- (5)}
\]

\[
V = \alpha_0 + \beta_1 D^2 + \beta_2 H + \beta_3 D^2 H + \varepsilon_i \quad \text{----------------------------- (6)}
\]

Where \( V \) = merchantable volume (m\(^3\)); \( D \) = dbh/stump diameter (cm); \( H \) = merchantable height (m); \( \varepsilon_i \) = error estimate and \( \alpha_0, \beta_1, \beta_2 \text{ and } \beta_3 \) = regression coefficients.

2.3.4 Criteria for Model Assessment

The following criteria were used in assessing the fitted equations:

(a) Significance of regression equation using the F-ratio test statistics. The F-ratio is an indication of whether or not the regression equation may be used for prediction. It is given by:

\[
F = \frac{\text{Regression Mean Square}}{\text{Error Mean Square}} \quad \text{----------------------------- (7)}
\]

The critical value of F (i.e. \( F_{\text{tabulated}} \)) at \( \alpha = 0.05 \) level is \( F(v_1, v_2) \), where \( v_1 \) and \( v_2 \) are degrees of freedom for regression and error, respectively. Where the variance ratio (F-calculated) is greater than the F-tabulated, the Null hypothesis is not accepted, and it is concluded that regression is significant. This implies that the regression equation may be used for prediction. The contrary holds where the F-calculated is less than the F-tabulated.

(b) The coefficient of determination (\( R^2 \)): It measures the proportion of variation in the dependent variable that has been accounted for by the linear relationship to the independent variables. \( R^2 \) is expressed as:
\[ R^2 = \frac{\text{Regression Sum of Square}}{\text{Total Sum of Square}} \]  \hspace{2cm} (8)

The coefficient of determination lies between zero and one (i.e. \( 0 \leq R^2 \leq 1 \)). If the decimal fraction is large (i.e. close to 1), most of the variability is accounted for by the relationship, and the regression equation is therefore a good prediction equation. If \( R^2 \) is close to zero the linear model is a poor fit to the data and the regression equation is therefore not very useful.

(c) Standard error of estimate (SEE) and the prediction sum of squares statistic (PRESS) were used to assess the volume equations. The equation(s) with the highest \( R^2 \) and lowest SEE were chosen and adjudged the best.

\[ \text{Where} \quad R^2 = 1 - \frac{\text{ESS}}{\text{TSS}} \]  \hspace{2cm} (9)

\[ \text{ESS} = \text{Error Sum of Square} \]
\[ \text{TSS} = \text{Total Sum of Square} \]
\[ \text{SEE} = \sqrt{\frac{\text{ESS}}{n-p}} \]  \hspace{2cm} (10)

\( n = \) number of observations
\( p = \) number of estimated coefficient

The final models chosen were analysed with a scatter diagram of the residuals over the range of the independent variable to investigate if assumption of independence of residuals is valid and shows conformity with the assumption of independence of errors in regression analysis. That is to investigate if error is normally distributed. The relationships between the variables were also analysed graphically and correlated to show degree of linearity.

3. Result and Discussion

3.1 Preliminary Data Analysis

Out of total of 1,419 trees that were measured, 364 trees were identified as belonging to leguminosae family. 199 of the trees were identified in Afi River Forest Reserve and 165 trees identified in Oban Forest Reserve. Three sub-families (caesalpinioideae, mimosoideae and papilionoideae) of leguminosae were encountered in the study areas. 10 tree species were identified as belonging to caesalpinioideae, while 7 and 5 tree species belong to mimosoideae and papilionoideae respectively (Table 1). Table 2 shows the result of preliminary data analysis of the trees variables and per hectare estimate. The results indicate that Afi River Forest Reserve and Oban Forest Reserve have an average number of trees per hectare to be 104 and 64 respectively. The numbers of trees per hectare obtained in this study is high in the two forest reserves when compare to the values reported by Adekunle et al, (2004) and Jimoh et al. (2011) for all families in mixed forest. The minimum dbh and stump diameter were 0.111m and 0.127m for Afi River Forest Reserve and 0.100m and 0.120m for Oban Forest Reserve respectively. The maximum dbh and stump diameter were 1.800m and 1.800m for
Afi River Forest Reserve and 1.20m and 1.32m for Oban Forest Reserve respectively. The mean dbh and stump diameter obtained are 0.643m and 0.704m respectively for Afi River Forest Reserve and 0.377m and 0.381m respectively for Oban Forest Reserve. The two forest types investigated in this study were characterized by abundance of trees with small dbh, especially in Oban Forest Reserve. This trend is not unusual for the tropical rainforests. Similar results have been reported by previous authors in other tropical rainforests of Nigeria (Adekunle et al., 2004; Adekunle and Olagoke, 2008). The reason for relatively fewer number of tree individuals of larger dbh values greater than 0.50m (dbh > 0.50m) can be attributed to limited number of species that naturally grow up to this diameters class (Hartshorn, 1980) and the numbers of certain big tree species could have been already reduced by selective extraction for some uses in the past (Hadi et al., 2009).

The minimum and maximum merchantable height obtained for Afi River Forest Reserve are 2.70m and 55m respectively while for Oban Forest Reserve are 2.00m and 40m respectively. The basal area/ha in this study was lesser in Oban Forest Reserve (8.19m$^2$) than the Afi River Forest Reserve (42.47m$^2$). The values obtained in the two forest types were reasonably compared to that suggested by Alder and Abayomi, (1994), for a well-stocked tropical rainforest in Nigeria. This is to be expected since the study area is under protection by law, with minimal human use pressure. The clear difference between basal area per hectare values of Afi River Forest Reserve and Oban Forest Reserve can be attributed to logging and farming activities which more prevalent in Oban Forest Reserve.

The merchantable volumes per hectare recorded for the Afi River Forest Reserve and Oban Forest Reserve are 1,088.80m$^3$ and 164.54m$^3$ respectively. The volume per hectare values recorded in this studies is an indication that the reserves are probably one of the richest of the tropical rainforest left in Nigeria when compare to the values reported by previous related researches carried out in other tropical rainforests of Nigeria (e.g. Adekunle et al., 2004; Adekunle and Olagoke, 2008). This may also be indication that, the reserves are probably well protected. The value recorded for Afi River Forest Reserve is higher than that recorded for Oban Forest Reserve. This implies that the Afi River Forest Reserve is better stocked than the Oban Forest Reserve.

Table 1. Results of grouping the 22 tree species by sub-families

<table>
<thead>
<tr>
<th>Group 1 Caesalpinioideae</th>
<th>Group 2 Mimosoideae</th>
<th>Group 3 Papilosoideae</th>
</tr>
</thead>
<tbody>
<tr>
<td>Afzelia Africana</td>
<td>Albizia ferruginea</td>
<td>Amphimas pterocarpoides</td>
</tr>
<tr>
<td>Berolina grandiflora</td>
<td>Albizia gumifera</td>
<td>Baphia nitida</td>
</tr>
<tr>
<td>Brachystegia eurycoma</td>
<td>Albizia zygia</td>
<td>Pentaclethra macrophylla</td>
</tr>
<tr>
<td>Daniellia ogea</td>
<td>Cylicodiscus gabunensis</td>
<td>Pterocarpus osun</td>
</tr>
<tr>
<td>Detarium macrocarpum</td>
<td>Parkia bicolour</td>
<td>Pterocarpus soyauxii</td>
</tr>
<tr>
<td>Distemonanthus benthamianus</td>
<td>Piptadeniastrum africanum</td>
<td></td>
</tr>
</tbody>
</table>
Table 2. Summary statistics of the major growth characteristics in the study areas.

<table>
<thead>
<tr>
<th></th>
<th>Afi River Forest Reserve</th>
<th>Oban Forest Reserve</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Number of trees/hectare</strong></td>
<td>104</td>
<td>64</td>
</tr>
<tr>
<td><strong>Dbh (m)</strong></td>
<td>0.111 - 1.800</td>
<td>0.100 - 1.200</td>
</tr>
<tr>
<td><strong>Dst (m)</strong></td>
<td>0.127 - 1.800</td>
<td>0.120 - 1.322</td>
</tr>
<tr>
<td><strong>MTH (m)</strong></td>
<td>2.700 - 55.000</td>
<td>2.000 - 40.000</td>
</tr>
<tr>
<td><strong>Basal Area (m²/ha)</strong></td>
<td>24.84 - 1535.90</td>
<td>24.97 - 609.67</td>
</tr>
<tr>
<td><strong>Merchantable Vol/ha (m³/ha)</strong></td>
<td>586.50 - 1535.90</td>
<td>609.67 - 164.54</td>
</tr>
</tbody>
</table>

Dbh - diameter at breast height, Dst - Outside bark stump diameter, Vol - volume

3.2 Relationship among Variables

The correlation matrix of the growth attribute for the two forest reserves is presented in Tables 3 and 4. The correlation coefficient shows strongest relationship between dbh and stump, which proved that stump diameter can be a substitute for dbh in tree volume estimation. Similar results have been reported for Pines and Oaks (Bylin, 1982), Teak (Osho, 1983), Bald Cypress (Parresol, 1998) and *Gmelina arborea* (Akindele, 2003) while lowest relationship is between basal area and merchantable height, which to an extent proved that merchantable height is not really a direct factor for size of basal area of tree.

Table 3. Correlation matrix of growth attribute of Afi River Forest Reserve

<table>
<thead>
<tr>
<th></th>
<th>dbh/m</th>
<th>Db/m</th>
<th>THT/m</th>
<th>MHT/m</th>
<th>BA/m²</th>
<th>MVol/m³</th>
</tr>
</thead>
<tbody>
<tr>
<td>dbh/m</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Dst/m</td>
<td>0.992611</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>THT/m</td>
<td>0.85229</td>
<td>0.858945</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MHT/m</td>
<td>0.764036</td>
<td>0.766196</td>
<td>0.876695</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BA/m²</td>
<td>0.970369</td>
<td>0.95876</td>
<td>0.805122</td>
<td>0.715887</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>MVol/m³</td>
<td>0.876599</td>
<td>0.871098</td>
<td>0.757936</td>
<td>0.762453</td>
<td>0.912689</td>
<td>1</td>
</tr>
</tbody>
</table>
Table 4. Correlation matrix of growth attribute of Oban Forest Reserve

<table>
<thead>
<tr>
<th></th>
<th>dbh/m</th>
<th>Db/m</th>
<th>THT/m</th>
<th>MHT/m</th>
<th>BA/m2</th>
<th>MV ol/m3</th>
</tr>
</thead>
<tbody>
<tr>
<td>dbh/m</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Dst/m</td>
<td>0.991817</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>THT/m</td>
<td>0.811514</td>
<td>0.800097</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MHT/m</td>
<td>0.750243</td>
<td>0.736653</td>
<td>0.948065</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BA/m2</td>
<td>0.951905</td>
<td>0.951525</td>
<td>0.711379</td>
<td>0.62835</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>MV ol/m3</td>
<td>0.91158</td>
<td>0.916879</td>
<td>0.751416</td>
<td>0.69265</td>
<td>0.9592</td>
<td>1</td>
</tr>
</tbody>
</table>

3.2 Volume Equations for All Species Combined

The volume equations for all species combined using dbh and stump diameter multiple variables are presented in equation 11 and 12 respectively. The two equations that were adjudged the best out of the several equations fitted were the logarithmic Schumacher equations of the following forms:

For model form:  
\[ \ln V = \alpha_0 + \beta_1 \ln (Dbh^2H) + \varepsilon_i \]

\[ \ln V = -0.48205 + 0.9939 \ln (Dbh^2H) \]  

\[ R = 0.990, R^2 = 0.980, R^2_{adj} = 0.980, F \text{ ratio} = 17,673.88, \text{SEE} = 0.2398 \]

For model form:  
\[ \ln V = \alpha_0 + \beta_1 \ln (Dst^2H) + \varepsilon_i \]

\[ \ln V = -0.78963 + 1.0391 Dst^2H \]  

\[ R = 0.990, R^2 = 0.980, R^2_{adj} = 0.980, F \text{ ratio} = 17,938.57, \text{SEE} = 0.2381 \]

3.3 Volume Equations for the Species Groups

The method of species grouping in this study was morphological and based on sub-families of tree species. Several empirical equations were fitted using dbh and stump diameter multiple-variable volume equations. The best equations that were adjudged the best (which is the logarithmic schumacher equation) are presented in Tables 5 and 6. The two tables indicate that the intercept of the equation for all the groups pass through the negative y-axis. As noted by Avery and Burkhart (1994), for merchantable volume prediction, negative intercepts are expected. In this study, D^2H as weighting factor was found to be appropriate in reducing heteroscedasticity. Similar remarks have been made by several authors including Cunia (1964), Snowdon (1985), Philip (1994) and Akindele (2005). The model being significant indicates a good fits and confirmed the effectiveness of weighted predictor in stabilising error.
variance. The results of the single-variable volume equations, using stump diameter only as predictor variable is presented in Table 7. From a series of model-fitting trials, the logarithmic non-linear function performed best within the limit of data used for each species group.

Table 5. Regression statistics for the volume equation for each species group

Model Form: \( \ln V = \alpha_0 + \beta_1 \ln (D_{bh}^2 H) + \varepsilon_i \)

<table>
<thead>
<tr>
<th>Group</th>
<th>( a_0 )</th>
<th>( b_1 )</th>
<th>( R )</th>
<th>( R^2 )</th>
<th>( R^2_{\text{adj}} )</th>
<th>SEE</th>
<th>F ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-0.471</td>
<td>0.985</td>
<td>0.987</td>
<td>0.975</td>
<td>0.975</td>
<td>0.277</td>
<td>7183.93</td>
</tr>
<tr>
<td>2</td>
<td>-0.502</td>
<td>1.006</td>
<td>0.994</td>
<td>0.988</td>
<td>0.988</td>
<td>0.165</td>
<td>9427.70</td>
</tr>
<tr>
<td>3</td>
<td>-0.475</td>
<td>0.998</td>
<td>0.992</td>
<td>0.983</td>
<td>0.983</td>
<td>0.241</td>
<td>3319.05</td>
</tr>
</tbody>
</table>

Table 6. Regression statistics for the volume equation for each species group

Model Form: \( \ln V = \alpha_0 + \beta_1 \ln (D_{st}^2 H) + \varepsilon_i \)

<table>
<thead>
<tr>
<th>Group</th>
<th>( a_0 )</th>
<th>( b_1 )</th>
<th>( R )</th>
<th>( R^2 )</th>
<th>( R^2_{\text{adj}} )</th>
<th>SEE</th>
<th>F ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-0.793</td>
<td>1.033</td>
<td>0.988</td>
<td>0.976</td>
<td>0.976</td>
<td>0.269</td>
<td>7593.15</td>
</tr>
<tr>
<td>2</td>
<td>-0.819</td>
<td>1.056</td>
<td>0.992</td>
<td>0.985</td>
<td>0.985</td>
<td>0.185</td>
<td>7509.13</td>
</tr>
<tr>
<td>3</td>
<td>-0.738</td>
<td>1.034</td>
<td>0.993</td>
<td>0.985</td>
<td>0.985</td>
<td>0.228</td>
<td>3723.06</td>
</tr>
</tbody>
</table>

Table 7. Regression statistics for the volume equation for each species group

Model Form: \( \ln V = \alpha_0 + \beta_1 \ln D_{st} + \varepsilon_i \)

<table>
<thead>
<tr>
<th>Group</th>
<th>( a_0 )</th>
<th>( b_1 )</th>
<th>( R )</th>
<th>( R^2 )</th>
<th>( R^2_{\text{adj}} )</th>
<th>SEE</th>
<th>F ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.79</td>
<td>2.701</td>
<td>0.972</td>
<td>0.945</td>
<td>0.945</td>
<td>0.500</td>
<td>3171.83</td>
</tr>
<tr>
<td>2</td>
<td>2.87</td>
<td>2.751</td>
<td>0.976</td>
<td>0.952</td>
<td>0.951</td>
<td>0.329</td>
<td>2289.30</td>
</tr>
<tr>
<td>3</td>
<td>3.00</td>
<td>3.050</td>
<td>0.973</td>
<td>0.945</td>
<td>0.945</td>
<td>0.435</td>
<td>978.28</td>
</tr>
</tbody>
</table>

4. Conclusion

The limiting factor in developing volume equation for mixed tropical rainforest is dearth of data which impairs the development of reliable species-specific volume equations. This problem can be surmounted by aggregating the species into groups and then developing appropriate equations for each species group. Species grouping was done by dividing the species into sub families and developed volume equations for each sub-families of leguminosae.

The generalised logarithmic volume function (also termed Schumacher’s volume function) performed better than other forms of volume functions. The equations developed in this study should be very useful in all cases of pre and post-harvest assessment of trees of leguminosae family and can be useful for stock assessment and planning. Developing volume equations from stump diameter is useful in the event that if there is illegal felling of tree, the stump left
on ground can determine what is removed and offenders appropriately charged. It advisable to use tree volume equations for species groups due to relatively large number of observations instead of the species-specific equations for which sample size was small. The estimation of merchantable tree volumes is essential for understanding of allowable cut cycle and for establishing sustainable forest management in forest reserves. Further and more comprehensive study in this area is recommended. More studies are needed to achieve more applied results.

Reference


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