

Effective Learning of Mathematics by Year 7 Students using the Bar Model Method: Case of Brunei Students

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Abstract

Mathematics is one of the challenging subjects in the Brunei education system. Achievement rate in this subject is often low especially among males. Both barriers and enablers of success need to be identified early to help fix the problem. The present field survey (N = 254 randomly selected Year 7 students, 144 males and 110 females) examined the: (1) attitudes and perceptions of students towards the Bar Model Method (BMM) of teaching and learning mathematics; (2) predictors of achievement in mathematics; and (3) effectiveness of the BMM in teaching and learning mathematics. Both genders and age-groups had positive attitudes and perceptions towards the BMM. In addition, the majority of participants (all genders, age-groups and districts) stated that the BMM was effective and liked the strategy. Furthermore, the participants' Word Problem-Solving Achievement Test (WPSAT) posttest scores did not differ significantly by gender and age-group. However, students in Brunei-Muara and Kuala Belait districts scored significantly higher at the posttest level than those in Tutong. Two implications were drawn from this finding. First, schools in Tutong might not be well-resourced like those in the other two districts. Second, more BMM work with students was required in Tutong to facilitate mastery of the strategy.

Keywords: Bar Model Method, attitudes, perceptions, predictors, effectiveness



Introduction

The Bar Model Method (BMM) uses bar diagrams to model facts given in a word problem (Walker, 2005; 2006). Walker (2005) stressed and contended that the approach was useful in organizing information. According to Yeap (2010), the BMM helps students solve arithmetic and algebraic word problems. He further said that the procedure was a common problem-solving heuristic used in Singapore schools. The BMM is ideal as a 'linking' method for problem solving in mathematics from one level to the next (Huat & Huat, 2001). Studies (e.g. Bishop, 1989; Veloo & Lopez, 1994; Fong, 1997; and Huat & Huat, 2001) indicate that the model helps students to visualize situations, create concrete pictures from abstract situations, and transform words into recognizable pictures for the mind to analyze. According to Huat and Huat (2001), the introduction of model drawing involves six stages of representation before the box diagrams are used. This method is taught to primary school children in Singapore (Ng & Lee, 2009). The method is embedded into the primary mathematics curriculum. According to Kho (1987; 2009) the model can be used as a tool for solving both arithmetic and algebraic word problems involving whole numbers, fractions, ratios and percentages. Once students understood the structure of the problem, they were more likely to be able to solve it (Kho, 1987; 2009). The purpose of this study is therefore to investigate the effectiveness of the BMM strategy in enhancing the mathematics achievement and problem solving skills among the secondary school students in Brunei Darussalam. Specifically, the research sought to understand how primary school children could, through experience, effectively learn mathematics using the BMM to improve performance (Suffolk & Gurung, 2005). The BMM could help students in understanding and solving different types of mathematical problems (Navan, 1998; Mohiddin, 2001; Mawang, 2001).

Learning and teaching psychological research on Brunei education system

This is the first time research was done about the effectiveness of the BMM strategy of teaching and learning mathematics with young students in Brunei. Past research of a psychoeducation nature had addressed a number of problems such as various disabilities (Bradshaw & Mundia, 2005; Bradshaw & Mundia, 2006; Tait & Mundia, 2012a, b; Haq & Mundia, 2012; Mundia, 2006; Yusuf & Mundia, 2014; Tait & Mundia, 2014; Tait, Mundia, & Fung, 2014; Tait, Mundia, Fung, & Wong, (2014). Besides disability, previous research also examined the mental health concerns of students in the education system (Mundia 2010a; Mundia, 2010b; Mundia 2012a, b; Mundia, 2013; Mundia, 2015). Most of the teaching and learning research on Brunei has focused on a wide range of school subjects including mathematics and Japanese language (Mundia, 1998; Mundia, 2010c; Mundia, 2010d; Mundia, 2007; Mundia, (2009); Mundia, 2011a; Mundia, 2012c; Keaney & Mundia, 2014). The training of teachers was also accorded priority by research (e.g. Mundia, 2012d, e; Tait & Mundia, 2012b; Tait & Mundia, 2014). Problems associated with conducting research using Brunei student samples were investigated by two studies (see Mundia & Bakar, 2010; Mundia, 2011b).

Research Questions

The present study investigated the following seven research questions (RQs):



RQ1: Do Year 7 students' attitudes towards the BMM strategy differ significantly by gender?

RQ2: Is there a significant difference in Year 7 students' attitudes to the BMM strategy by age-group?

RQ3: Are Year 7 students in different districts significantly different in attitudes towards the BMM strategy?

RQ4: What variables are significantly related to Year 7 students' achievement in mathematics when using the BMM strategy while learning?

RQ5: Were there significant differences by gender, age and district in Year 7 students' perceptions of how challenging the use of the BMM strategy in solving mathematics word problem was?

RQ6: Did Year 7 students differ significantly by gender, age and district in their opinions about the effectiveness of the BMM strategy in solving mathematics word problems?

RQ7: Do Year 7 students' mathematics WPSAT scores differ significantly by gender, age and district before and after using the BMM strategy?

Method

The methodology for the present study comprised of the design, participants, instruments, data analysis techniques, and procedures, each of which is briefly explained below.

Design

We used a mixed methods design incorporating a quantitative field survey and a pretest-posttest experiment. These procedures enabled the researchers to collect the needed data from a big sample timely.

Sample

Participants of the study consisted of 254 Year 7 students representing both genders and chosen from different schools by the simple random selection procedure. Table 1 profiles selected characteristics of the participants by gender, age-group, and district. Temburong district was excluded since it has only one school.



Variable	Group	Frequency	Percentage
	27.1		
Gender	Male	144	56.7
	Female	110	43.3
Age-group	11 – 12 years	211	83.1
	13 – 14 years	43	16.9
District	Brunei-Muara	183	72.0
	Kuala Belait	44	17.3
	Tutong	27	10.6

Table 1. Demographic information of the Year 7 Students (N = 254)

Instruments

The data for the current study were collected by three instruments presented in Table 2. The positive and negative attitudes questionnaires to BMM were both Likert scales with a 4-point response format (1SD, 2D, 3A, 4SA). The reliability for these two instruments was assessed by alpha method. As its name implies, the Word Problem-Solving Achievement Test (WPSAT) consisted of worded mathematics items that students had to solve manually. The response to each item was coded as: 0 (when wrong) and 1 (if correct). Partially correct responses were not taken into consideration. The WPSAT was administered as both a pretest and posttest to the same group of learners before and after students learnt mathematics using the BMM. We used the Kuder-Richardson 21 (KR21) procedure to determine the reliability of the WPSAT. The theoretical assumption underpinning this internal consistency method requires items to have nearly the same difficulty level (Ary *et al.*, 2002). Failure to meet this assumption or violation of it, will result in the procedure underestimating the reliability of the test and thereby giving a lower-bound value. To avoid this problem, we picked 10 items with p-values or facility indices of about 0.50 from a pool of 17 WPSAT questions that we pretested. All the instruments were reliable as shown in Table 2.

Table 2. Descriptive statistics and	reliability of the instruments (N=254))
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Scales	Items	Mean	SE Mean	SD	Reliability
Positive attitudes to BMM	17	46.350	0.526	8.394	0.891 ^a
Negative attitudes to BMM	5	11.300	0.151	2.412	0.719 ^a
Word Problem-Solving Achievement Test (WPSAT)– Pretest	10	1.750	0.201	3.207	0.955 ^b
Word Problem-Solving Achievement Test (WPSAT)– Posttest	10	3.780	0.262	4.180	0.962 ^b

^aCronbach alpha

^bKuder-Richardson 21 (KR21)

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With regard to the validity of the instruments, the two attitude scales (positive and negative attitudes to the BMM) correlated negatively and significantly [r(254) = -0.290, p < .01, two-tailed]. This significant negative relationship provided quantitative evidence that the two scales had adequate discriminant validity. On the other hand, pretest and posttest scores from the Word Problem-Solving Achievement Test (WPSAT) correlated positively and significantly $[r_{prepost}(254) = 0.713, p < .01, two-tailed]$. The significant positive relationship demonstrated that the pre-post scores had sufficient convergent validity.

Procedures

The present study was funded by the Government of Brunei Darussalam in form of a doctoral study grant to the first author at the University of Brunei Darussalam (UBD). In turn, the University of Brunei Darussalam Ethics Committee approved the study on behalf of the government. Furthermore, ethical conditions and rights (e.g. anonymity, confidentiality, privacy, voluntary participation, protection from harm, and informed consent) for participating in the study were first explained verbally in both English and Bahasa Melayu language to individual research participants' parents and school authorities prior to collecting the data from young students. After this, verbal and written informed consent were secured from each research participant's parents in either of the two languages at the time and place of collecting the data. Only students whose parents voluntarily agreed to let their children be involved in the study were recruited to participate. Coercion and deception were not used when recruiting the participants. Furthermore, all the study's research tools were written in simple English language requiring only Grade 7 or Year 7 level of education. To address and reduce any possible linguistic and cultural biases, parallel bilingual items were presented on the instruments in both English and Bahasa Melayu, the main and official language of Brunei spoken by the majority of the people. Above all, data collection occurred in in the participants' school environments to increase the study's ecological validity.

Data analysis

Data were analyzed using descriptive statistics (frequencies, percentages, mean, and standard deviation) and inferential statistics (Pearson correlations, independent groups t-tests, X^2 , and hierarchical multiple regression analysis). To determine the importance of our findings, we used two-tailed tests of statistical significance at both p = 0.05 and p = 0.01 levels and tests of statistical power such as R² (for multiple regression analysis, effect sizes (for t-tests and One-Way ANOVA analyses), and phi coefficients (for chi-square analyses). All the statistical analyses were performed on SPSS Version 22.

Results

The results are presented below according to the research questions probed. Tables were used to summarize the findings.

RQ1: Do Year 7 students' attitudes towards the BMM strategy differ significantly by gender?

No statistically significant differences were obtained by gender. In relative terms however, Table 3 shows that the female students had more positive attitudes than males.

Scales	Males (n=145	5)	Females (n=109)		ANCOVA	Т	Р	ŋ
_	Mean	SD	Mean	SD	F	(df=252)	(two-tailed)	
Positive Attitudes	45.74	8.498	47.16	8.183	0.091	-1.331	0.184	0.084
Negative Attitudes	11.34	2.343	11.25	2.502	0.212	0.295	0.768	0.019

Table 3. Year 7 students' attitudes towards the BMM strategy by gender (N=254)

RQ2: Is there a significant difference in Year 7 students' attitudes to the BMM strategy by age-group?

There were no statistically significant differences by age-groups as shown by evidence in Table 4.

Table 4. Year 7 students' attitudes towards the BMM strategy by age (N=254	4)
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Scales	11-12 Years		13-14 Years		ANCOVA	т	р		
Scales	(n=211)	(n=43)		ANCOVA	1	P	ŋ	
	Mean	SD	Mean	SD	F	(df=252)	(two-tailed)		
Positive Attitudes	46.64	8.075	44.91	9.705	1.519	1.241	0.216	0.078	
Negative Attitudes	11.24	2.373	11.58	2.584	0.280	-0.843	0.400	0.053	

RQ3: Are Year 7 students in different districts significantly different in attitudes towards the BMM strategy?

As indicated in Table 5, students in Kuala Belait district scored significantly higher on positive attitudes scale towards the BMM than peers in Brunei-Muara and Tutong districts $[F(df = 2, 253) = 7.924, p < .001, \eta = 0.244]$. This difference was associated with an appreciable effect size.

Scales	Brunei-Muara (n=183)	Kuala Belait (n=44)	Tutong (n=27)	F (<i>df</i> =2, 253)	P (two-tailed)	ŋ	
	Maan (SD)	Mean	Mean				
	Mean (SD)	(SD)	(SD)				
Positive	45.59	50.73	44.37	7.924	0.000***	0.244	
Attitudes	(8.409)	(7.488)	(7.396)	1.924	0.000***	0.244	
Negative	11.44	10.95	10.93	1.076	0.343	0.092	
Attitudes	(2.426)	(2.372)	(2.336)	1.070	0.343	0.092	

Table 5. Year 7 students' attitudes towards the BMM Strategy by district (N=254)

***p<.001 (two-tailed)

RQ4: What variables were significantly related to Year 7 students' achievement in



mathematics when using the BMM strategy while learning?

Hierarchical multiple regression analysis with backward elimination was used to identify predictors of mathematics achievement when students were taught using the BMM strategy. Four independent or predictor variables (negative attitudes, gender, positive attitudes, and age) were entered and regressed on mathematics achievement scores (response or dependent variable) in Model 1. The analysis was completed after three iterations or steps. The first required output are presented in Table 6. Model 1 was significant and accounted for 80.6% of the common variance between the independent variables and dependent variable.

Table 6. Prediction of Year 7 students' mathematics achievement using hierarchical regression with backward elimination (N=254)

df	F	R	R^2	Adj R ² SE		Chang	hange Statistics			
						ΔR^2	ΔF	dfl	df2	Sig.∆F
4, 254	259.327***	0.898	0.806	0.803	1.259	0.806	259.327	4	250	0.000***
3, 254	346.682	0.898	0.806	0.803	1.257	0.000	0.273	1	250	0.602
2, 254	519.480	0.897	0.805	0.803	1.257	-0.001	1.017	1	251	0.314
	4, 254 3, 254		4, 254 259.327*** 0.898 3, 254 346.682 0.898	4, 254 259.327*** 0.898 0.806 3, 254 346.682 0.898 0.806	4, 254 259.327*** 0.898 0.806 0.803 3, 254 346.682 0.898 0.806 0.803	4, 254 259.327*** 0.898 0.806 0.803 1.259 3, 254 346.682 0.898 0.806 0.803 1.257	$\frac{1}{\Delta R^2}$ 4, 254 259.327*** 0.898 0.806 0.803 1.259 0.806 3, 254 346.682 0.898 0.806 0.803 1.257 0.000	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	ΔR^2 ΔF dfl 4, 254 259.327*** 0.898 0.806 0.803 1.259 0.806 259.327 4 3, 254 346.682 0.898 0.806 0.803 1.257 0.000 0.273 1	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

*** p<.001 (two-tailed)

After removing and adjusting for gender and negative attitudes, the two good predictors of mathematics achievement were age and positive attitudes. Of these, the best predictor was positive attitudes as indicated in Table 7.

Table 7. Predictors of Year 7 students' mathematics achievement using hierarchical regression with backward elimination (N=254)

		Unstandardi	zed	Standardized		
Model	Variables	Coefficients		Coefficients	t	Sig.
		В	Std. Error	Beta		
	Gender	0.170	0.155	0.091	1.097	0.274
1	Age	-0.255	0.174	-0.198	-1.467	0.144
1	Positive Attitudes	0.064	0.007	1.059	8.632	0.000***
	Negative Attitudes	s-0.015	0.028	-0.060	-0.523	0.602
	Gender	0.152	0.151	0.081	1.008	0.314
2	Age	-0.305	0.145	-0.237	-2.101	0.037*
	Positive Attitudes	0.063	0.007	1.049	8.676	0.000***
3	Age	-0.272	0.141	-0.211	-1.922	0.054*
3	Positive Attitudes	0.066	0.007	1.100	10.011	0.000***

*p<.05 (two-tailed)

***p<.001 (two-tailed)

RQ5: Were there significant differences by gender, age and district in Year 7 students' perceptions of how challenging the use of the BMM strategy in solving mathematics word problem was?



No significant differences were obtained by gender. According to Tables 8, the BMM strategy was neither easy nor difficult to use.

Statement	Easy F (M)†	Neutral F (M)	Difficult F (M)	χ ²	df	Phi	Р
How easy/difficult was it to use the BMM strategy to solve mathematics word problem?	45 (55)	45 (56)	19 (34)	1.368	2	0.073	0.504
+ E = Eomolog: M = Molog							

Table 8. Year 7 students' perceptions of the use of BMM strategy by gender (N=254)

 $\dagger F = Females; M = Males$

However, there were significant differences by age. Table 9 shows that most of the younger students aged 12 years and below either found the BMM to be easy or were neutral with no opinion on this matter [χ^2 (df = 2) = 6.282, @ = 0.157, p<.05].

Table 9. Year 7 students' Perceptions of the use of BMM strategy by Age (N=254)

Statement	Easy A(B)†	Neutral A(B)	Difficult A(B)	χ^2	df	Phi	Р
How easy/difficult was it to use the BMM strategy to solve mathematics word problem?	87 (13)	86 (15)	38 (15)	6.282	2	0.157	0.043

 $\dagger A = 12$ years old and below; B = 13 years old and above

According to Table 10, no significant differences were obtained by districts as indicated by the chi-square and phi coefficients.

Table 10. Year 7 students'	perceptions on use of the	BMM strategy by district (N=254)
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Statement	Easy 1 (2) 3 †	Neutral 1 (2) 3	Difficult 1 (2) 3	χ^2	df	Phi	Р
How easy/difficult was it to use	75	70	38				
the BMM strategy to solve	(17)	(21)	(6)	4.749	4	0.137	0.314
mathematics word problem?	8	10	9				
	17 1	D 1 1					

†1= Brunei-Muara; (2) = Tutong; 3 = Kuala Belait

RQ6: Did Year 7 students differ significantly by gender, age and district in their opinions about the effectiveness of the BMM strategy in solving mathematics word problems?

Tables 11, shows that Year 7 students did not differ significantly by gender in their opinions about the effectiveness of the BMM strategy in solving mathematics word problems.



Table 11. Year 7 students' opinions on the effectiveness of the BMM strategy by gender (N=254)

How effective do you think the BMM strategy is for 15 47 47 0.273 2 0.033 0. solving mathematics word (22) (58) (65) 0.273 2 0.033 0.	Statement	Ineffective F (M)†	Neutral F (M)	Effective F (M)	χ^2	df	Phi	Р
1	the BMM strategy is for				0.273	2	0.033	0.873

 $\dagger F = Females; M = Males$

With regards to the students' opinions in terms of their age, Table 12 shows no significant difference.

Table 12. Year 7 students' of	opinions on the effectiveness	s of the BMM strategy by age (N=254)

Statement	Ineffective A (B) †	Neutral A (B)	Effective A (B)	χ^2	df	Phi	Р
How effective do you think the BMM strategy is for solving mathematics word problem?		91 (14)	87 (25)	4.266	2	0.130	0.118

 $\dagger A = 12$ years old and below; (B) = 13 years old and above

In addition, Year 7 students did not also differ significantly by district in their opinions about the effectiveness of the BMM strategy in solving mathematics word problems (see Table 13).

Table 13. Year 7 students' opinions on the effectiveness of the BMM strategy by district (N=254)

Statement	Ineffective 1 (2) 3†	Neutral 1 (2) 3	Effective 1 (2) 3	χ^2	df	Phi	Р
How effective do you think the BMM strategy is for solving mathematics word problem?	26 (3) 8	76 (19) 10	81 (22) 9	7.252	4	0.169	0.123

†1= Brunei-Muara; (2) = Tutong; 3 = Kuala Belait

Comparison of the students' Word Problem-Solving Achievement Test (WPSAT) pre-post scores when using the BMM

RQ7: Do Year 7 students' mathematics WPSAT scores differ significantly by gender, age and district before and after using the BMM strategy?

Based on the findings presented in Tables 14, Year 7 students' mathematics WPSAT scores did not differ significantly by gender before and after using the BMM strategy.

Assessments	Males (n=144	4)	Female (n=110		ANCOVA	Т	Р	ES
	Mean	SD	Mean	SD	F	(df=252)	(two-tailed)	
Pretest scores	1.660	3.261	1.870	3.145	0.369	-0.524	0.601	0.033
Posttest scores	3.570	4.240	4.050	4.102	0.663	-0.916	0.360	0.058

Table 14. Independent-sample t-test comparison of the WPSAT scores by gender (N=254)

Tables 15 also shows that Year 7 students' WPSAT mathematics scores did not differ significantly by age before and after using the BMM strategy.

Table 15. Independent-sample t-test comparison of the WPSAT scores by age (N=254)

Assessments	11-12 (n=211		13-14 (n=43)		ANCOVA	Т	Р	ES
	Mean	SD	Mean	SD	F	(df=252)	(two-tailed)	
Pretest scores	1.770	3.266	1.670	2.934	0.127	0.174	0.862	0.011
Posttest scores	3.940	4.271	2.980	3.635	4.193	1.384	0.167	0.087

However, Year 7 students' WPSAT mathematics scores differed significantly by district before and after using the BMM strategy as indicated in Table 16. At the pretest level, students in Muara-Brunei district scored significantly higher than peers in Kuala Belait and Tutong districts [F(df = 2, 253) = 3.107, p<.05, $\eta = 0.155$]. For the posttest phase, students in both Kuala Belait and Brunei-Muara districts scored significantly much higher than their counterparts in Tutong district [F(df = 2, 253) = 6.067, p<.01, $\eta = 0.215$].

Table 16. One-Way ANOVA comparison of the WPSAT scores by district (N=254)

Assessments	Brunei-Muara (n=183)	Kuala Belait (n=44)	Tutong (n=27)	F (df=2, 253)	P (two-tailed)	ŋ	
	Mean	Mean	Mean				
	(SD)	(SD)	(SD)				
Pretest scores	2.02	1.45	0.44	3.107	0.046*	0 155	
Fieldst scores	(3.220)	(3.763)	(1.281)	5.107	0.040	0.155	
Posttest scores	4.07	4.18	1.19	6.067	0.003**	0.215	
Positest scores	(4.214)	(4.597)	(1.711)	0.007	0.003	0.215	

*p< 0.05 (two-tailed)

**p< 0.01 (two-tailed)

Discussion

Both genders and age-groups scored high on positive attitudes toward the BMM strategy in this study. In addition, both genders and age-groups also scored low on negative attitudes toward the BMM. Taken together, these two findings suggested that the majority of the study participants liked the BMM method of teaching and learning mathematics. The BMM appeals to students because it allows them to visualize the problem and think about it concretely before solving it (see Bishop, 1989; Veloo & Lopez, 1994; Fong, 1997; and Huat & Huat,



2001).

All the participants in the three districts scored low on negative attitudes toward the BMM technique but high on positive attitudes. However, students in Kuala Belait had significantly higher positive attitudes toward the BMM than those in Brunei-Muara and Tutong. In general, these findings concur with the attitudinal outcomes discussed above in terms of gender and age-groups but also imply that more BMM work needs to be done with students in Brunei-Muara and Tutong districts. Often it takes a bit of time for students and teachers to get used to the BMM approach for teaching and learning mathematics (Walker, 2005; 2006). Once students and teachers get used to it, the procedure yield good achievement results as in Singapore where it has been in operation for many years (Yeap, 2010).

The strongest and best predictor of mathematics achievement in this study was positive attitudes towards the BMM procedures. Age (a categorical variable) predicted achievement negatively with younger students who learn better with concrete materials and reasoning liking the BMM more than their older peers. The BMM is one several factors that researchers and teachers could help students in understanding and solving different types of mathematical problems (Nayan, 1998; Mohiddin, 2001; Mawang, 2001).

Participants of both genders and age-groups residing in all the three districts held favorable perceptions of the BMM strategy. However, younger students (who prefer learning using concrete materials) had more favorable perceptions compared to their older counterparts. This finding is in agreement with previous research which says the BMM helps students to visualize situations, create concrete pictures from abstract situations, and transform words into recognizable pictures prior to solving the problem (e.g. Bishop, 1989; Veloo & Lopez, 1994; Fong, 1997; and Huat & Huat, 2001). With regard to the effectiveness of the BMM strategy, the majority of participants (all genders, age-groups, and districts) thought that it was effective. The success of many primary and secondary school students in mathematics in Singapore has been largely credited to the use of the BMM approach of teaching and learning (Ng & Lee, 2009; Yeap, 2010).

Evidence from the current study's pre-post experiment showed no significant differences on posttest scores by gender and age on the Word Problem Solving Achievement Test (WPSAT) of mathematics. The elimination of major differences on performance associated with these demographic variables may be attributed to the effectiveness of the BMM strategy for teaching and learning mathematics for young students. Once students understood the structure of the problem through visual or pictorial representation of the data, they were more likely to be able to solve the problem concretely (Kho, 1987; 2009). However, students in Brunei-Muara and Kuala Belait districts scored significantly higher at the posttest level than those in Tutong. This difference might be due to two factors. First, there more students in Brunei-Muara and Kuala Belait districts than in Tutong. Second, the finding calls for more BMM work to be done with mathematics struggling students in Tutong.

Conclusion

There is ample evidence from the present study indicating that the BMM would be helpful in



improving mathematics achievement in Brunei Year 7 students. The BMM should therefore be included in teacher education curriculum for both pre-service and in-service training programs. In this way, teachers would be skilled to use the method efficiently during mathematics instruction.

Limitations

The present study had two main limitations. First, we did not include an interview component with probes to explore further the participants' responses from the quantitative surveys. Second, the sample size was only moderate. Despite these shortcomings, the current study's findings have practical significance that may be relevant to policy-makers and researchers in Brunei and elsewhere.

Declarations

Abbreviations

UBD: University of Brunei Darussalam; SPSS: Statistical Package for Social Sciences

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Competing interests

The authors declare that they did not have any conflict of interests

Ethics approval and consent to participate

Permission to conduct the study was obtained from the University of Brunei Darussalam Ethics Committee

Consent for publication and permissions to reproduce material

Not applicable. The authors declare that they did not use any materials that needed permission from the copyright owners

Authors' contributions

The authors contributed equally to the article

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Requests for data

The data cannot be released without permission from the participants. Contact the corresponding author on reasonable requests for access to the data

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